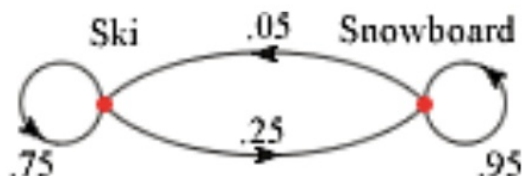


6.1 Matrix Representations

Transition diagram



Transition matrix



This entry shows that 5% of people who snowboard today will ski tomorrow.



First week

IC 220

FY 20

Second week

$220(-.95) + 20(.10) = 211$

Next wk.

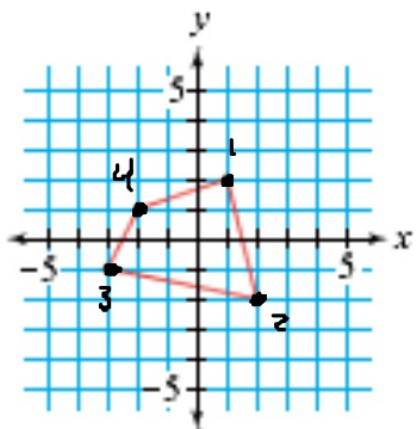
IC

FY

IC .95 .05

FY .10 .90

Ex. A



$$\begin{matrix} x \\ y \end{matrix} \begin{bmatrix} 1 & 2 & -3 & -2 \\ 2 & -2 & -1 & 1 \end{bmatrix}$$

→ Rows
↓ Columns

entry

dimensions = rows x columns

2x4 matrix

1x3

$[a \ b \ c]$

entry 1, 2 = 2

3x1

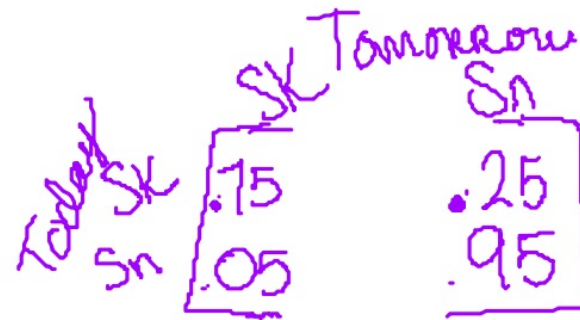
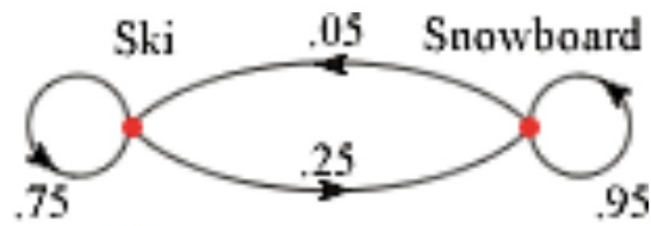
$\begin{bmatrix} a \\ b \\ c \end{bmatrix}$

entry 2, 3 = -1

entry row, column

1 = entry 2, 4

Ex. B



Day 1: 260 Skiers
40 Snowboarders

Day 2: 260 SK
 $\times .75$
195

40 SN
 $\times .05$
2

197 SK
103 Snowboarders

260
- 195
65

40
- 2
38

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1-4, 11



3)

$$S_k \begin{bmatrix} .60 & .40 \end{bmatrix} = 1.00$$

$$S_n \begin{bmatrix} .53 & .47 \end{bmatrix} = 1.00$$

4)

$A \quad B \quad C$

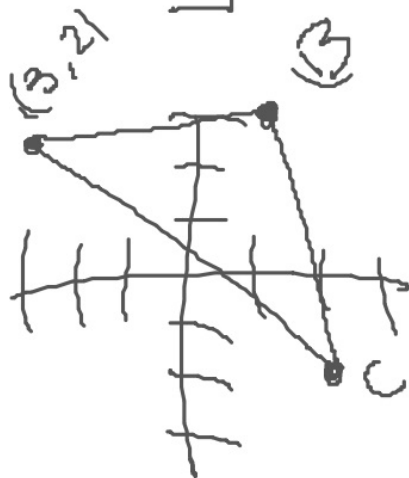
$$X \begin{bmatrix} -3 & 1 & 2 \end{bmatrix}$$

$$Y \begin{bmatrix} 2 & 3 & -2 \end{bmatrix}$$

$A(-3, 2)$

$B(1, 3)$

$C(2, -2)$



$$\begin{bmatrix} 1, 1 & 1, 2 \\ 2, 1 & 2, 2 \end{bmatrix}$$

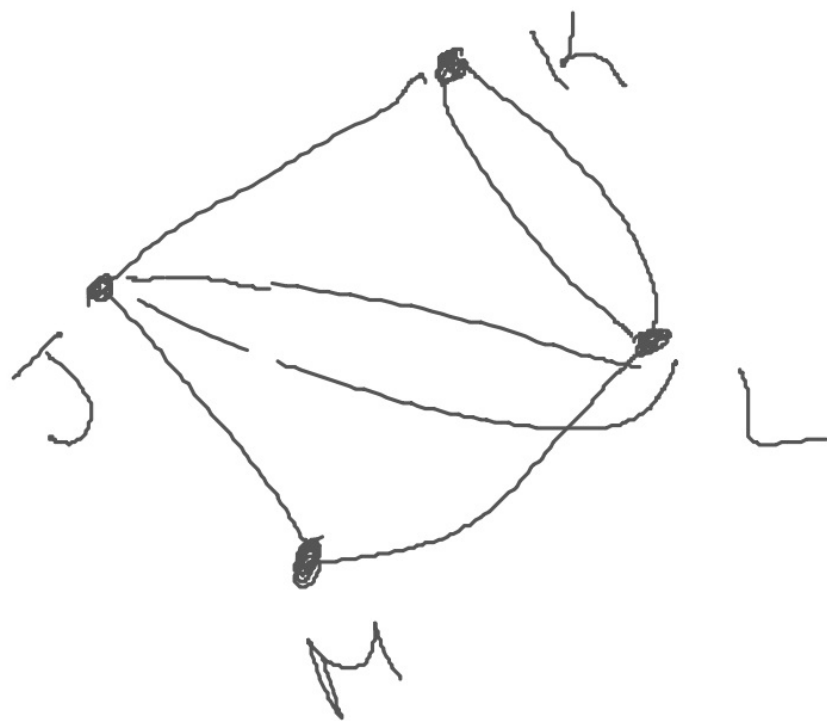
$A'(-3, -2) \quad A''(1, 2)$

$B'(1, -1) \quad B''(5, 3)$

$C'(2, -6) \quad C''(6, -2)$

$$\begin{array}{c}
 J \\
 K \\
 L \\
 M
 \end{array}
 \begin{bmatrix}
 0 & 1 & 2 & 1 \\
 1 & 0 & 2 & 0 \\
 2 & 2 & 0 & 1 \\
 1 & 0 & 1 & 0
 \end{bmatrix}
 = \begin{array}{c}
 3 \\
 5
 \end{array}$$

J K L M



$$[A] = \begin{bmatrix} 86 & 33 \\ 65 & 20 \\ 78 & 50 \end{bmatrix}$$

$$[B] = \begin{bmatrix} 80 & 25 \\ 65 & 15 \\ 105 & 55 \end{bmatrix}$$

$$[A] + [B] = \begin{bmatrix} 166 & 58 \\ 130 & 35 \\ 203 & 105 \end{bmatrix}$$

$$[C] = \begin{bmatrix} 12 & 69 \\ 82 & 82 \\ 71 & 71 \end{bmatrix}$$

$$[D] = \begin{bmatrix} 72 \\ 15 \\ 6 \end{bmatrix}$$

Cannot
be
added

$$\begin{bmatrix} 1 & 1 \\ 1 & 1 \\ 1 & 1 \end{bmatrix}$$

$$3 \times 2$$

$$1 \times 3$$

$$3 \times 1$$

$$\begin{bmatrix} 0 \\ 6 \\ 0 \end{bmatrix}$$

$$2 \times 3$$

$$[A] + [B]$$

Ex A $\begin{bmatrix} -3 & 1 & 2 \\ 2 & 3 & -2 \end{bmatrix}$ Left 3 units $\begin{bmatrix} -6 & -2 & -1 \\ 2 & 3 & -2 \end{bmatrix}$

trans. $\begin{matrix} \xrightarrow{+} + \\ \xleftarrow{-} - \end{matrix}$ $\begin{matrix} \uparrow + \\ \downarrow - \end{matrix}$ $+ \begin{bmatrix} -3 & -3 & -3 \\ 0 & 0 & 0 \end{bmatrix} = \begin{bmatrix} -6 & -2 & -1 \\ 2 & 3 & -2 \end{bmatrix}$

b) $\begin{bmatrix} -3 & 1 & 2 \\ 2 & 3 & -2 \end{bmatrix} + \begin{bmatrix} -4 & -4 & -4 \\ -3 & -3 & -3 \end{bmatrix} = \begin{bmatrix} -7 & -3 & -2 \\ -1 & 0 & -5 \end{bmatrix}$

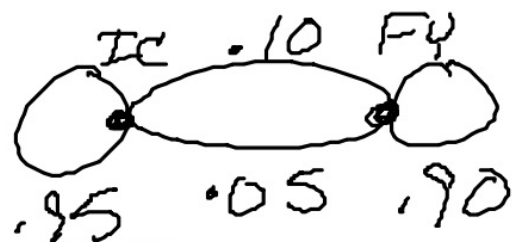
c) $\frac{1}{2} \cdot \begin{bmatrix} -3 & 1 & 2 \\ 2 & 3 & -2 \end{bmatrix} = \begin{bmatrix} -6 & 2 & 4 \\ 4 & 6 & -4 \end{bmatrix}$ dilation

Constriction

$\bigcirc \rightarrow \bigcirc$

$\bigcirc \rightarrow 0$

Ex B



$$\begin{bmatrix} 200 & 20 \end{bmatrix}_{1 \times 2} \begin{bmatrix} .95 & .05 \\ .10 & .90 \end{bmatrix}_{2 \times 2} = \begin{bmatrix} 192 & 28 \end{bmatrix}$$

Diagram showing the matrix multiplication of a 1×2 row vector $[200 \ 20]$ with a 2×2 matrix $\begin{bmatrix} .95 & .05 \\ .10 & .90 \end{bmatrix}$ to produce a 1×2 row vector $[192 \ 28]$. Arrows indicate the mapping of the 200 value to the $.95$ and $.10$ entries, and the 20 value to the $.05$ and $.90$ entries.

$$\begin{array}{r}
 \left[\begin{array}{cc} 200 \times .95 & 200 \times .05 \\ 20 \times .10 & 20 \times .90 \end{array} \right] \\
 \hline
 \left[192 \quad 28 \right]
 \end{array}$$

Multiply

Columns = rows
 1×2

2×2

2×2

2×2

2×3

2×3

2×3

3×3

1×2

3×1

Ex C

$$\begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}_{2 \times 2} \begin{bmatrix} -3 & 1 & 2 \\ 2 & 3 & -2 \end{bmatrix}_{2 \times 3} = \begin{bmatrix} 3 & -1 & -2 \\ 2 & 3 & -2 \end{bmatrix}_{2 \times 3}$$

must match

1×2 2×2

$$\left[\begin{array}{r} -1 \cdot -3 \\ + 0 \cdot -3 \\ \hline 3 \end{array} \quad \begin{array}{r} -1 \cdot 1 \\ + 0 \cdot 1 \\ \hline -1 \end{array} \quad \begin{array}{r} -1 \cdot 2 \\ + 0 \cdot 2 \\ \hline -2 \end{array} \right]$$

$$\left[\begin{array}{r} 2 \cdot 0 \\ + 1 \cdot 2 \\ \hline 2 \end{array} \quad \begin{array}{r} 3 \cdot 0 \\ + 1 \cdot 3 \\ \hline 3 \end{array} \quad \begin{array}{r} -2 \cdot 0 \\ + 1 \cdot -2 \\ \hline -2 \end{array} \right]$$

$$8) \quad [A] = \begin{bmatrix} 2 & 3 \\ -1 & 1 \end{bmatrix} \quad [B] = \begin{bmatrix} 3 & 4 \\ 0 & -2 \end{bmatrix} \quad [C] = \begin{bmatrix} -2 & 3 & 0 \\ -1 & 5 & 4 \end{bmatrix} \quad [D] = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \quad 4/26$$

$$a) \quad [A][B] = \begin{bmatrix} 6 & 2 \\ -3 & -6 \end{bmatrix}$$

$$[B][A] = \begin{bmatrix} 2 & 13 \\ 2 & -2 \end{bmatrix}$$

$$b) \quad [A][C] = \begin{bmatrix} -7 & 21 & 12 \\ 1 & 2 & 4 \end{bmatrix}$$

$$2 \times 3 \quad 2 \times 2$$

$$[C][A] = \text{Dimension mismatch}$$

$$8 \quad [A] = \begin{bmatrix} 2 & 3 \\ -1 & 1 \end{bmatrix} \quad [B] = \begin{bmatrix} 3 & 4 \\ 0 & -2 \end{bmatrix} \quad [C] = \begin{bmatrix} -2 & 3 & 0 \\ -1 & 5 & 4 \end{bmatrix} \quad [D] = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$c) [A][D] = \begin{bmatrix} 2 & 3 \\ -1 & 1 \end{bmatrix} = [A]$$

$$[D][A] = \begin{bmatrix} 2 & 3 \\ -1 & 1 \end{bmatrix} = [A]$$

Multiplication Identity = 1

Identity Matrix

in echelon

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

Matrix Addition

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- Must be the same size

- add corresponding entries (eg. $1,1 + 1,1$)

Scalar Multiplication

Multiply the number by every entry

Matrix Multiplication

- Columns from first matrix must match rows from second matrix

(eg. $\overset{C}{1 \times 2} \overset{R}{2 \times 2}$) $\begin{bmatrix} 1,1 & 1,2 \end{bmatrix} \begin{bmatrix} 1,1 & 1,2 \\ 2,1 & 2,2 \end{bmatrix}$

- multiply $1,1 + 1,2$ from first

by $1,1 + 2,1$ from 2nd - Sum the corresponding

- Continue across second matrix entries

$$4 \begin{bmatrix} 8 & -5 & 4.5 \\ -6 & 9.5 & 5 \end{bmatrix} - [B] = \begin{bmatrix} 5 & -1 & 2 \\ -4 & 3.5 & 1 \end{bmatrix}$$

2 \times 3

$$\begin{bmatrix} \underline{3} & \underline{-4} & \underline{2.5} \\ \underline{\quad} & \underline{\quad} & \underline{\quad} \end{bmatrix}$$

- A system of equations that has at least one solution is called **consistent**.
- A system of equations that has no solutions is called **inconsistent**.
- A system with infinitely many solutions is called **dependent**.
- A system of equations that has exactly one solution is called **independent**.

augment — to add to

$$2x + y = 5$$

$$5x + 3y = 13$$

$$3x \begin{array}{cc|c} x & y & \text{answer} \\ \hline 2 & 1 & 5 \\ 5 & 3 & 13 \end{array}$$

$$\begin{bmatrix} 6 & 3 & | & 15 \\ 5 & 3 & | & 13 \end{bmatrix} R_1 - R_2$$

$$\begin{bmatrix} 1 & 0 & | & 2 \\ 5 & 3 & | & 13 \end{bmatrix} R_2 - 5R_1$$

$$\begin{bmatrix} 1 & 0 & | & 2 \\ 0 & 3 & | & 3 \end{bmatrix} \div 3$$

$$\begin{bmatrix} 1 & 0 & | & 2 \\ 0 & 1 & | & 1 \end{bmatrix} \begin{array}{cc|c} x & y & \text{answer} \end{array}$$

$$y = 2 \quad (2, 1)$$

$$\begin{array}{cc} y = 1 \\ x & y \\ \begin{bmatrix} 0 & 1 & | & 1 \\ 1 & 0 & | & 2 \end{bmatrix} \end{array}$$

$$(2x + y = 5) \times 3$$

$$5x + 3y = 13$$

$$6x + 3y = 15$$

$$-5x + 3y = 13$$

$$1x + 0y = 2$$

$$1 \quad 0 \quad | \quad 2$$

$$2(2) + y = 5$$

$$4 + y = 5$$

$$y = 1$$

$$5x \begin{bmatrix} 2 & 1 & | & 5 \\ 5 & 3 & | & 13 \end{bmatrix}$$

$$2x \begin{bmatrix} 10 & 5 & | & 25 \\ 10 & 6 & | & 26 \end{bmatrix}$$

$$R_2 - R_1 \begin{bmatrix} 10 & 5 & | & 25 \\ 0 & 1 & | & 1 \end{bmatrix}$$

$$\div 10 \begin{bmatrix} 10 & 0 & | & 20 \\ 0 & 1 & | & 1 \\ 1 & 0 & | & 2 \\ 0 & 1 & | & 2 \end{bmatrix}$$

$$7x + 2y = 11$$

$$3x - 5y = 120$$

$$2.5 \times \begin{bmatrix} 7 & 2 & | & 11 \\ 3 & -5 & | & 120 \end{bmatrix}$$

$$\begin{bmatrix} -3.5 & 5 & | & -120 \\ 20.5 & 0 & | & 147.5 \end{bmatrix} \div -3.5$$

$$\begin{bmatrix} 1 & -1.428 & | & 34.29 \\ 20.5 & 0 & | & 147.5 \end{bmatrix}$$

$$\begin{bmatrix} 17.5 & 5 & | & 27.5 \\ 3 & -5 & | & 120 \end{bmatrix} R_1 + R_2$$

$$\begin{bmatrix} 17.5 & 5 & | & 27.5 \\ 1 & 0 & | & 7.2 \end{bmatrix}$$

$$\begin{bmatrix} 17.5 & 5 & | & 27.5 \\ 20.5 & 0 & | & 147.5 \end{bmatrix} R_1 - R_2$$

$$R_1 - 17.5 R_2 \quad \times 1/2$$

$$\begin{bmatrix} 0 & 5 & | & -98.5 \\ 1 & 0 & | & 7.2 \end{bmatrix}$$

$$\begin{bmatrix} 0 & 5 & | & -98.5 \\ 1 & 0 & | & 7.2 \end{bmatrix} R_1 \div 5$$

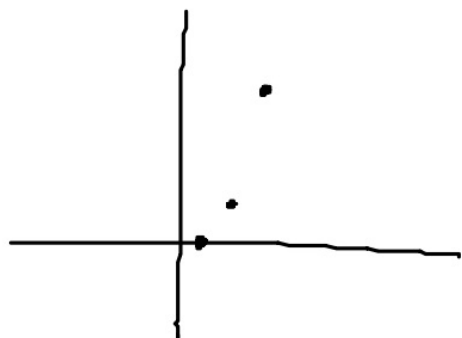
$$\begin{bmatrix} 0 & 1 & | & -19.7 \\ 1 & 0 & | & 7.2 \end{bmatrix}$$

$$(7.2, -19.7)$$

Inv. •

looks like x^2

$$ax^2 + bx + c = y$$



$R_3 - R_2$

$$\begin{bmatrix} 1 & 1 & 1 & | & 0 \\ 16 & 4 & 1 & | & 12 \\ 36 & 6 & 1 & | & 30 \end{bmatrix}$$

$R_3 \div 2$

$$\begin{bmatrix} 1 & 1 & 1 & | & 0 \\ 16 & 4 & 1 & | & 12 \\ 20 & 2 & 0 & | & 18 \end{bmatrix}$$

$$\left[\begin{array}{ccc|c} 1 & 1 & 1 & 0 \\ 16 & 4 & 1 & 12 \\ 10 & 1 & 0 & 9 \end{array} \right] R_2 - R_1$$

$R_3 - R_2$
 \downarrow

$$\left[\begin{array}{ccc|c} 1 & 1 & 1 & 0 \\ 15 & 3 & 0 & 12 \\ 10 & 1 & 0 & 9 \end{array} \right] R_2 / 3 \quad \left[\begin{array}{ccc|c} 1 & 1 & 1 & 0 \\ 5 & 1 & 0 & 4 \\ 10 & 1 & 0 & 9 \end{array} \right]$$

$$\begin{bmatrix} 1 & 1 & 1 & | & 0 \\ 5 & 1 & 0 & | & 4 \\ 5 & 0 & 0 & | & 5 \end{bmatrix} R_2 - R_3$$

$$R_1 - R_3 \begin{bmatrix} 1 & 0 & 1 & | & 1 \\ 0 & 1 & 0 & | & -1 \\ 1 & 0 & 0 & | & 1 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 1 & 1 & | & 0 \\ 0 & 1 & 0 & | & -1 \\ 5 & 0 & 0 & | & 5 \end{bmatrix} R_3 / 5$$

$$\begin{bmatrix} 0 & 0 & 1 & | & 0 \\ 0 & 1 & 0 & | & -1 \\ 1 & 0 & 0 & | & 1 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 1 & 1 & | & 0 \\ 0 & 1 & 0 & | & -1 \\ 1 & 0 & 0 & | & 1 \end{bmatrix} R_1 - R_2$$

$$1x^2 - 1x + 0 = 4$$

Ex B 50 receipts 3 book titles

✓ \$14.00 X \$18.50 Y \$23.25 C

✓ Total = \$909.00

✓ 22 more of \$18.50 sold than \$23.25
How many of each sold?

$$Y - C = 22$$

$$14X + 18.5Y + 23.25C = 909$$

$$X + Y + C = 50$$

$$\left[\begin{array}{ccc|c} 0 & 1 & -1 & 22 \\ 14 & 18.5 & 23.25 & 909 \\ 1 & 1 & 1 & 50 \end{array} \right]$$

$$\left[\begin{array}{ccc|c} 0 & 1 & -1 & 22 \\ 14 & 18.5 & 23.25 & 909 \\ 1 & 1 & 1 & 50 \end{array} \right]$$

$$R_2 - 14R_3$$

$$\left[\begin{array}{ccc|c} 0 & 1 & -1 & 22 \\ 0 & 4.5 & 9.25 & 209 \\ 1 & 1 & 1 & 50 \end{array} \right]$$

$$R_3 - R_1$$

$$\left[\begin{array}{ccc|c} 0 & 1 & -1 & 22 \\ 0 & 4.5 & 9.25 & 209 \\ 1 & 0 & 2 & 28 \end{array} \right]$$

$$R_2 \div 4.5$$

$$\left[\begin{array}{ccc|c} 0 & 1 & -1 & 22 \\ 0 & 1 & 2.06 & 46.4 \\ 1 & 0 & 2 & 28 \end{array} \right]$$

$R_2 - R_1$

$$\left[\begin{array}{ccc|c} 0 & 1 & -1 & 22 \\ 0 & 0 & 1 & 7.47 \\ 1 & 0 & 2 & 28 \end{array} \right]$$

$R_2 + R_1$

$$\left[\begin{array}{ccc|c} 0 & 1 & -1 & 22 \\ 0 & 0 & 3.6 & 24.4 \\ 1 & 0 & 2 & 28 \end{array} \right]$$

$R_2 / 3.6$

$$\left[\begin{array}{ccc|c} 0 & 1 & 0 & 29.97 \\ 0 & 0 & 1 & 7.47 \\ 1 & 0 & 2 & 28 \end{array} \right]$$

$R_3 - 2R_2$

$$\begin{bmatrix} 0 & 1 & 0 & | & 29.97 \\ 0 & 0 & 1 & | & 7.97 \\ 1 & 0 & 0 & | & 12.06 \end{bmatrix}$$

$$x = 12$$

$$y = 30$$

$$c = 8$$

$$\frac{30}{12}$$

$$\frac{56}{12 \times 14}$$

$$12 \times 14$$

$$9 + 30 = 18.5$$

I ♥ Jennifer

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#1-5

$$\underline{1 \times 3} \times \underline{3 \times 2}$$

1 x 2 answer size

$$+ \begin{bmatrix} a & b \\ c & d \\ e & f \end{bmatrix}$$

$$\underline{4 \times 3} \times \underline{3 \times 2}$$

$$4 \times 2$$

$$a \times \frac{1}{a} = 1 \quad \text{Inverse}$$

$$\begin{bmatrix} a & b \\ c & d \end{bmatrix}$$

$$[A] \quad [A]^{-1} = 1 = [A]^T [A]$$

Identity

$$r \times \textcircled{c} \quad \textcircled{r} \times c$$

 $r = c$
square

$$a \times 1 = a$$

$$\begin{bmatrix} a & b \\ c & d \end{bmatrix} \begin{bmatrix} 3 & 2 \\ 4 & 1 \end{bmatrix} = \begin{bmatrix} 3 & 2 \\ 4 & 1 \end{bmatrix}$$

$$\begin{bmatrix} 2 & 1 \\ 4 & 3 \end{bmatrix} \begin{bmatrix} a & b \\ c & d \end{bmatrix} = \begin{bmatrix} 2 & 1 \\ 4 & 3 \end{bmatrix}$$

2 × 2 2 × 2

Identity

$$\begin{bmatrix} 2a+1c & 2b+1d \\ 4a+3c & 4b+3d \end{bmatrix} = \begin{bmatrix} 2 & 1 \\ 4 & 3 \end{bmatrix}$$

$$2a+c=2 \quad 2b+d=1$$

$$4a+3c=4 \quad 4b+3d=3$$

$$(2a + c = 2) \times 2$$

$$4a + 3c = 4$$

$$-(4a + 2c = 4)$$

$$0a + 1c = 0$$

$$c = 0$$

$$4a + 3(0) = 4$$

$$4a = 4$$

$$a = 1$$

$$\begin{bmatrix} a & b \\ c & d \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \text{ n.r.e.m.}$$

$$(2b + d = 1) \times 2$$

$$4b + 3d = 3$$

$$-(4b + 2d = 2)$$

$$0b + 1d = 1$$

$$d = 1$$

$$2b + 1 = 1$$

$$\frac{2b}{2} = \frac{0}{2}$$

$$b = 0$$

Identity Matrix

$$[I][A] = [A][I] = [A]$$

$[I] =$ Same dim. as $[A]$
reduced row echelon matrix $\begin{bmatrix} 1 & & \\ & \ddots & \\ & & 1 \end{bmatrix}$

$$\begin{array}{c} [A] \\ \begin{bmatrix} 1 & 6 & 14 \\ 4 & 9 & 3 \\ 8 & 12 & 0 \end{bmatrix} \end{array} \times \begin{array}{c} [I] \\ \begin{bmatrix} \underline{1} & \underline{0} & \underline{0} \\ \underline{0} & \underline{1} & \underline{0} \\ \underline{0} & \underline{0} & \underline{1} \end{bmatrix} \end{array} = \begin{array}{c} [A] \\ \begin{bmatrix} 1 & 6 & 14 \\ 4 & 9 & 3 \\ 8 & 12 & 0 \end{bmatrix} \end{array}$$

Inverse Matrix

$$[A][A]^{-1} = [A]^{-1}[A] = [I]$$

$$[A]^{-1} \quad \text{Same dim. as } [A]$$

$$\begin{matrix} [A] & [A]^{-1} \\ \begin{bmatrix} 2 & 1 \\ 4 & 3 \end{bmatrix} & \begin{bmatrix} a & b \\ c & d \end{bmatrix} \end{matrix} = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$2a + 1c = 1 \quad 2b + 1d = 0$$

$$4a + 3c = 0 \quad 4b + 3d = 1$$

$$(2a + 1c = 1) \times 2$$

$$4a + 3c = 0$$

$$-(4a + 2c = 2)$$

$$0a + 1c = -2$$

$$c = -2$$

$$2a + 1(-2) = 1$$

$$2a - 2 = 1$$

$$+2 \quad +2$$

$$\frac{2a}{2} = \frac{3}{2}$$

$$a = \frac{3}{2} = 1.5$$

$$\begin{bmatrix} 1.5 & -0.5 \\ -2 & 1 \end{bmatrix}$$

$$(2b + 1d = 0) \times 2$$

$$4b + 3d = 1$$

$$-(4b + 2d = 0)$$

$$0b + 1d = 1$$

$$d = 1$$

$$2b + 1(1) = 0$$

$$2b + 1 = 0$$

$$\frac{2b}{2} = \frac{-1}{2}$$

$$b = -0.5$$

$$\overset{[A]}{\begin{bmatrix} 2 & 1 \\ 4 & 3 \end{bmatrix}} \overset{[A]^{-1}}{\begin{bmatrix} 1.5 & -0.5 \\ -2 & 1 \end{bmatrix}} = \overset{[I]}{\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}}$$

Solving a system using an inverse matrix

$$[A][x] = [B]$$

$$[A]^{-1}[A][x] = [A]^{-1}[B]$$

$$[I][x] = [A]^{-1}[B]$$

$$[x] = [A]^{-1}[B]$$

$$[A] \Rightarrow [A]^{-1}$$

$$2x + 3y = 7$$

$$\begin{array}{rcl} x & = & 6 - 4y \\ +4y & & +4y \end{array}$$

$$x + 4y = 6$$

$$\begin{array}{c} [A] \\ \begin{bmatrix} 2 & 3 \\ 1 & 4 \end{bmatrix} \\ 2 \times 2 \end{array} \begin{array}{c} [x] \\ \begin{bmatrix} x \\ y \end{bmatrix} \\ 2 \times 1 \end{array} = \begin{array}{c} [B] \\ \begin{bmatrix} 7 \\ 6 \end{bmatrix} \\ 2 \times 1 \end{array}$$

$$\begin{array}{c} [A]^{-1} \\ \begin{bmatrix} 0.8 & -0.6 \\ -0.2 & 0.4 \end{bmatrix} \end{array}$$

$$[A]^{-1}[B] = \begin{bmatrix} 2 \\ 1 \end{bmatrix} = \begin{bmatrix} x \\ y \end{bmatrix}$$

$$[A]^{-1}[A][x] = [I][x] = [x]$$

$$2c + 1d + 2p = 11.85$$

$$1c + 2d + 1p = 9.00$$

$$2d + 3p = 12.35$$

* Pgs. 331-332 #1-6

$$[A] = \begin{bmatrix} 2 & 1 & 2 \\ 1 & 2 & 1 \\ 0 & 2 & 3 \end{bmatrix}$$

3x3

$$[X] = \begin{bmatrix} c \\ d \\ p \end{bmatrix}$$

3x1

$$[B] = \begin{bmatrix} 11.85 \\ 9.00 \\ 12.35 \end{bmatrix}$$

3x1

$$[A]^{-1} [B]$$

WRONG

$$= \begin{bmatrix} 3.7214 \\ 0.8714 \\ 3.5357 \end{bmatrix}$$

3x1

$$= \begin{bmatrix} 2.15 \\ 2.05 \\ 2.75 \end{bmatrix}$$

3x1

$$4a) \begin{bmatrix} 5 & 2 \\ 7 & 3 \end{bmatrix} \begin{bmatrix} 3 & -2 \\ -7 & 5 \end{bmatrix} \quad \begin{array}{cc} 15 & -10 \\ -14 & 10 \end{array} \quad \begin{array}{cc} 21 & -14 \\ -21 & 15 \end{array} \quad \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$

yes

$$5d) \begin{bmatrix} 1 & 2 \\ 2 & 4 \end{bmatrix}$$

$[A]^{-1}$ Does not exist

x^{-1}

Same line

$$\begin{array}{l} 1x + 2y \\ 2x + 4y \end{array}$$

$$6a) \begin{array}{l} 8x + 3y = 41 \\ 6x + 5y = 39 \end{array}$$

$$\begin{array}{c} [A] \\ \begin{bmatrix} 8 & 3 \\ 6 & 5 \end{bmatrix} \end{array} \begin{array}{c} [x] \\ \begin{bmatrix} x \\ y \end{bmatrix} \end{array} = \begin{array}{c} [B] \\ \begin{bmatrix} 41 \\ 39 \end{bmatrix} \end{array}$$

$$\begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 4 \\ 3 \end{bmatrix}$$

$$[x] = [A]^{-1}[B]$$

" $[A]^{-1} = \begin{bmatrix} \quad \end{bmatrix}$ from calculator "

is acceptable.

Augmented

$$\left[\begin{array}{c|c} \text{O} & \text{O} \end{array} \right] \Rightarrow \left[\begin{array}{c} \text{O} \end{array} \right] \begin{bmatrix} \text{O} \end{bmatrix} = \begin{bmatrix} \text{O} \end{bmatrix}$$

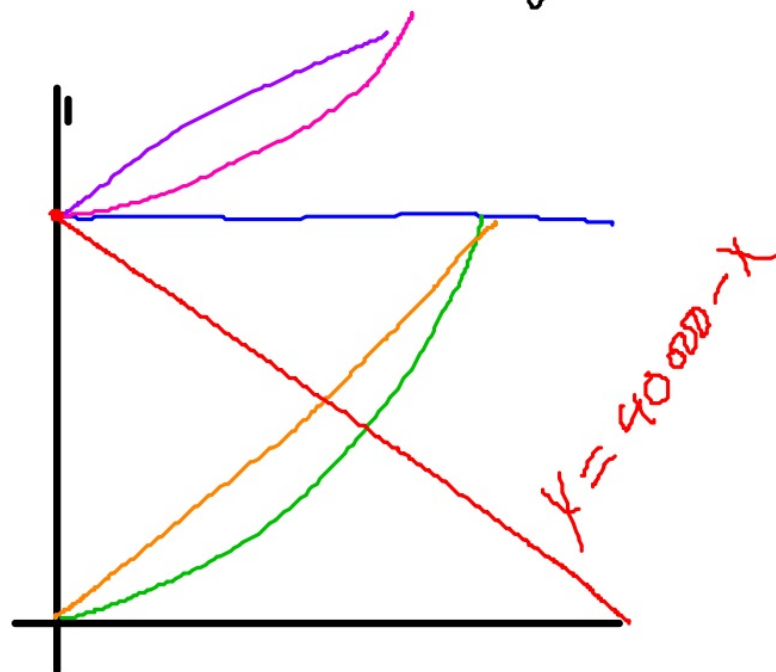
$\begin{matrix} \$ & & \$ & & \$ \\ 5 & \} & n & 5 & = & 1535 \end{matrix}$

$$n = -70 + 25$$

6.5 Systems of Linear Inequalities p. 336

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inequality = not equal
linear = straight line

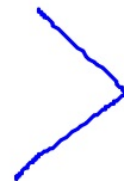
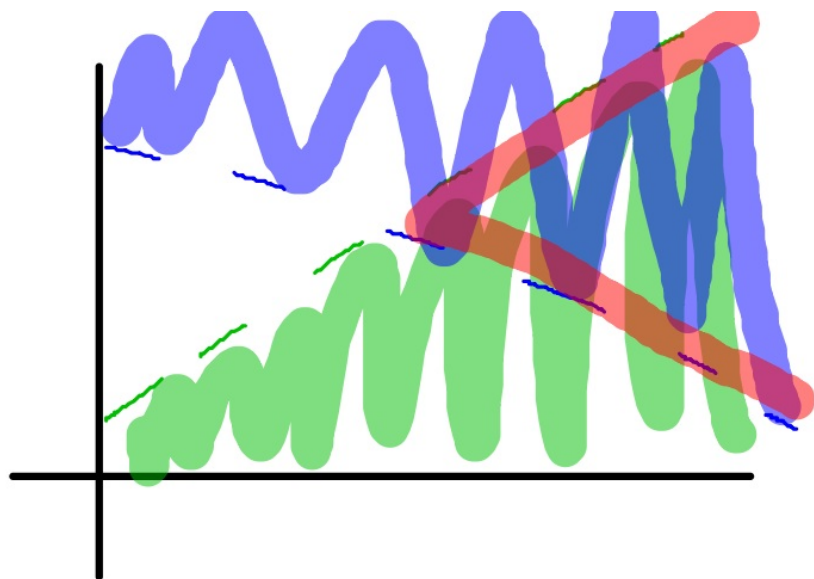


$$X + y = 40,000$$

$$y = 40000 - x$$

$< > \leq \geq$
inequalities





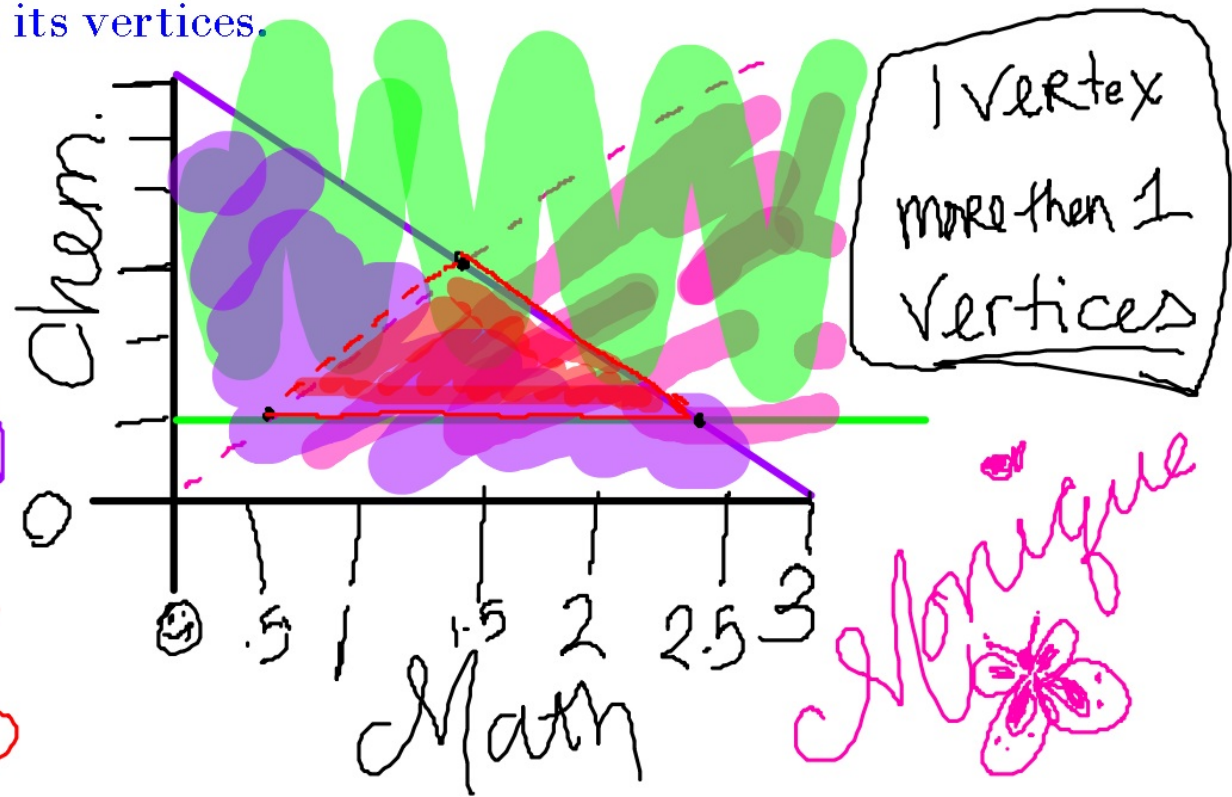
Rachel has 3 hours to work on her homework tonight. She wants to spend more time working on mathematics than on chemistry, and she must spend at least a half hour working on chemistry. State the constraints of this system algebraically with x representing mathematics time in hours and y representing chemistry time in hours. Graph your inequalities, shade the feasible region, and label its vertices.

$$x > y$$

$$0.5 \leq y$$

$$3 \geq x + y$$

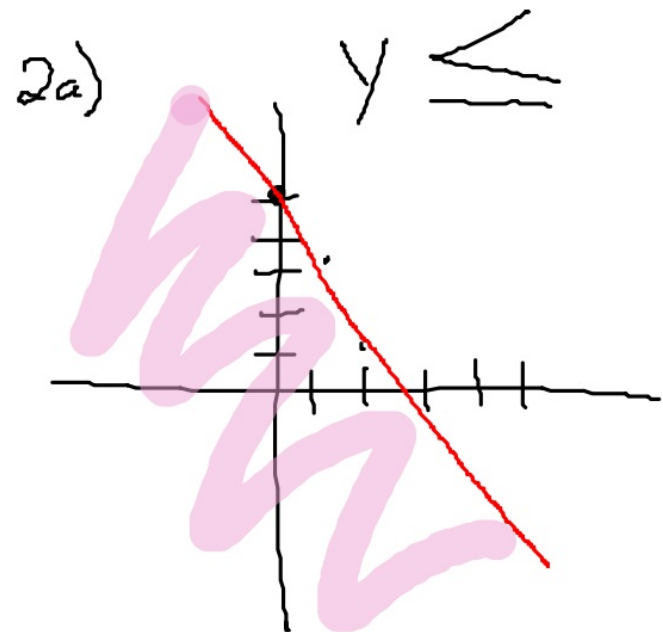
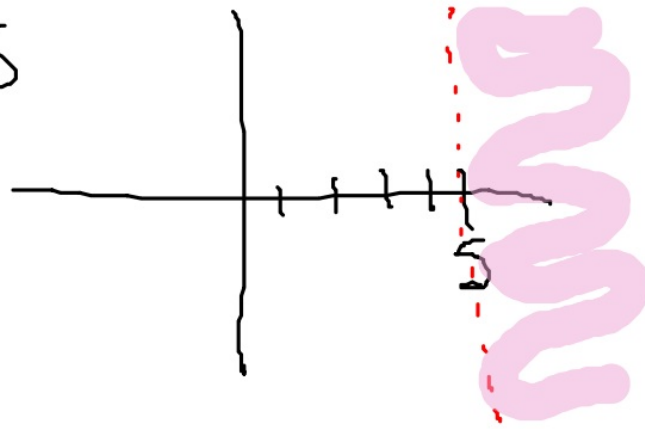
Homework #
Pg 339-340
#1, 2, 3, 5

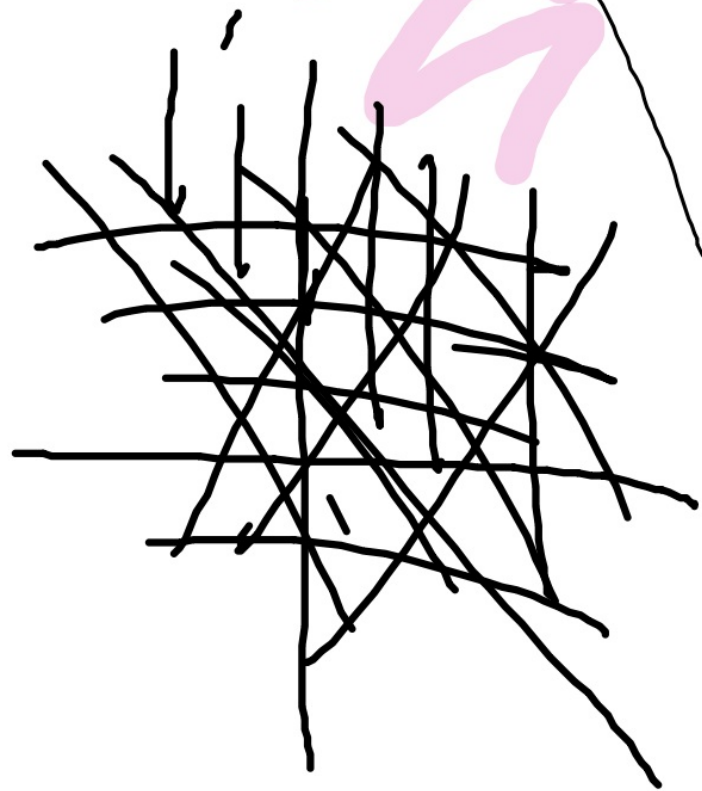
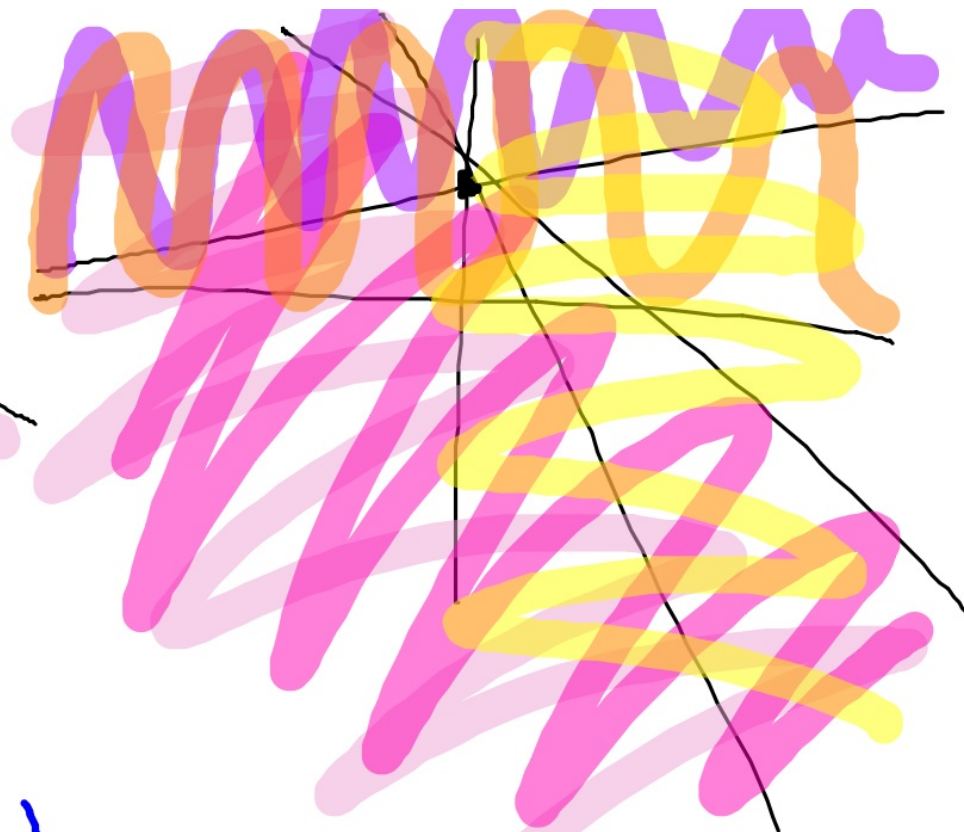


Inequalities are manipulated like equations EXCEPT when you multiply or divide by a NEGATIVE number. In those cases, the sign will flip from one direction to the other.

$$1a) \begin{array}{r} 2x - 5x > 10 \\ -2x \quad \quad -2x \\ \hline -5x > 10 - 2x \\ \hline -5 \quad \quad -5 \\ \hline y < -2 + \frac{2}{5}x \end{array}$$

$$2c) x \leq 5$$





3a)

$$y < 2 - \frac{1}{2}x$$

$$(0, 2) \quad (4, 0) \quad \frac{2}{4}$$

6.6 Linear Programming p. 344

5/16

linear programming - the process of finding a feasible region and determining the point that gives the maximum or minimum value to a specific expression

Considerations / Constraints

| | | |
|------------------------|----------------------|-------------|
| Kilns up to 60 h/d | $g_{\text{up to 2}}$ | $u_6 (18h)$ |
| pot. wheel up to 8 h/d | $g_{\text{up to 5}}$ | $u_6 (3h)$ |

u Unglazed min. 6 per day

| | | |
|----------------|-------|----------|
| Unglazed wheel | 0.5 h | 3.5 h ea |
| kiln | 3 h | |

g glazed wheel 1 h 19 h ea

| | | |
|------|------|--|
| kiln | 18 h | |
|------|------|--|

| | kiln | wheel | profit |
|--------------|-----------|----------|----------|
| glazed (g) | 18 | 1 | 40 |
| unglazed (u) | 3 | 0.5 | 10 |
| constraint | ≤ 60 | ≤ 8 | $u = 14$ |

$$18g + 3u \leq 60$$

$$1g + 0.5u \leq 8$$

$$g \leq 8 - 0.5u$$

$$18(8 - 0.5u) + 3u \leq 60$$

$$144 - 9u + 3u \leq 60$$

$$144 - 6u \leq 60$$

$$-6u \leq -84$$

$$u \geq 14$$

$$g + 0.5(14) \leq 8$$

$$g + 7 \leq 8$$

$$g \leq 1$$

$$18 + 1$$

$$42 + 7$$

$$14 + 14$$

$$18g + 3u \leq 60$$

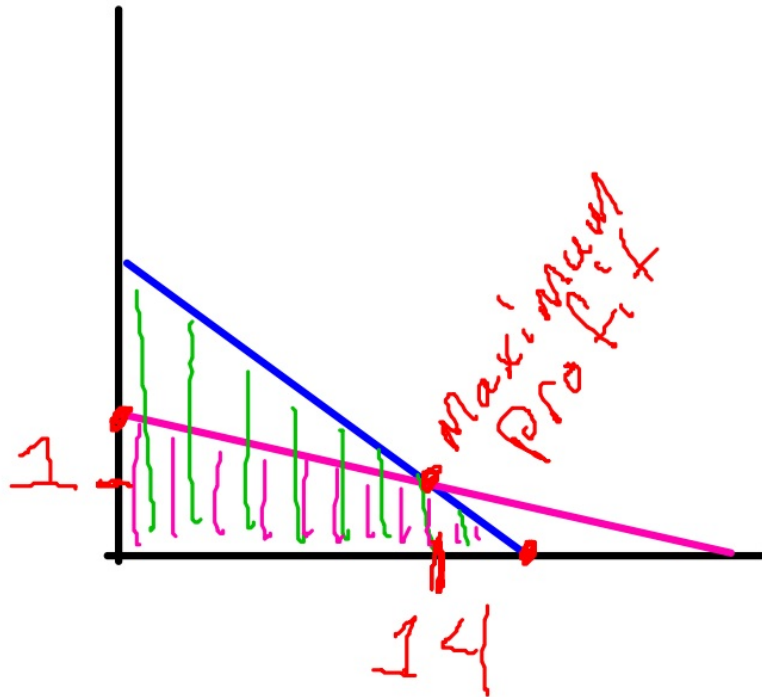
$$1g + 0.5u \leq 8$$

$$-g \leq (60 - 3u)/18 = 3.33 - .167u$$

$$-g \leq 8 - 0.5u \quad 5/17$$

$$u = 14$$

$$g = 1$$



p. 347
1-3

1, 2 a&c, 3-5, 7